## GCE Examinations Advanced Subsidiary

## **Core Mathematics C4**

Paper D

Time: 1 hour 30 minutes

## Instructions and Information

Candidates may use any calculator EXCEPT those with the facility for symbolic algebra, differentiation and/or integration.

Full marks may be obtained for answers to ALL questions.

Mathematical formulae and statistical tables are available.

This paper has seven questions.

## Advice to Candidates

You must show sufficient working to make your methods clear to an examiner. Answers without working may gain no credit.



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<b>1.</b> (a)	Find the binomial expansion of $(2-3x)^{-3}$ in ascending powers of $x$ up to and including the term in $x^3$ , simplifying each coefficient.	(5)
<i>(b)</i>	State the set of values of x for which your expansion is valid.	(1)

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2.	A curve has the equation		
	$x^2 + 3xy - 2y^2 + 17 = 0.$		
	(a) Find an expression for $\frac{dy}{dx}$ in terms of x and y.	(5)	
	(b) Find an equation for the normal to the curve at the point $(3, -2)$ .	(3)	

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**3.** (a) Find the values of the constants A, B, C and D such that

$$\frac{2x^3 - 5x^2 + 6}{x^2 - 3x} \equiv Ax + B + \frac{C}{x} + \frac{D}{x - 3}.$$
 (5)

(b) Evaluate

$$\int_{1}^{2} \frac{2x^3 - 5x^2 + 6}{x^2 - 3x} \, \mathrm{d}x,$$

	giving your answer in the form	$p + q \ln 2$ ,	where $p$ and $q$ are integers.	(5)
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4.	A mathematician is selling goods at a car boot sale. She believes that the rate at which she makes sales depends on the length of time since the start of the sale, $t$ hours, and the total value of sales she has made up to that time, £ $x$ .	
	She uses the model	
	$\frac{\mathrm{d}x}{\mathrm{d}t} = \frac{k(5-t)}{x},$	
	where $k$ is a constant.	
	Given that after two hours she has made sales of £96 in total,	
	(a) solve the differential equation and show that she made £72 in the first hour of the sale. (8)	
	The mathematician believes that is it not worth staying at the sale once she is making sales at a rate of less than £10 per hour.	
	(b) Verify that at 3 hours and 5 minutes after the start of the sale, she should have already left. (4)	

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**5.** Relative to a fixed origin, two lines have the equations

$$\mathbf{r} = \begin{pmatrix} 4 \\ 1 \\ 1 \end{pmatrix} + s \begin{pmatrix} 1 \\ 4 \\ 5 \end{pmatrix}$$

and

$$\mathbf{r} = \begin{pmatrix} -3\\1\\-6 \end{pmatrix} + t \begin{pmatrix} 3\\a\\b \end{pmatrix},$$

where a and b are constants and s and t are scalar parameters.

Given that the two lines are perpendicular,

(a) find a linear relationship between a and b. (2)

Given also that the two lines intersect,

- (b) find the values of a and b, (8)
- (c) find the coordinates of the point where they intersect. (2)

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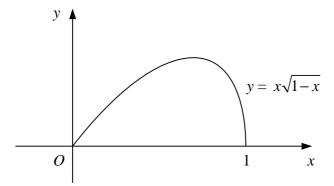


Figure 1

Figure 1 shows the curve with equation  $y = x\sqrt{1-x}$ ,  $0 \le x \le 1$ .

- (a) Use the substitution  $u^2 = 1 x$  to show that the area of the region bounded by the curve and the x-axis is  $\frac{4}{15}$ . (8)
- (b) Find, in terms of  $\pi$ , the volume of the solid formed when the region bounded by the curve and the x-axis is rotated through 360° about the x-axis. (5)

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7. A curve has parametric equations

$$x = 3\cos^2 t, \quad y = \sin 2t, \quad 0 \le t < \pi.$$

- (a) Show that  $\frac{dy}{dx} = -\frac{2}{3}\cot 2t$ . (4)
- (b) Find the coordinates of the points where the tangent to the curve is parallel to the x-axis. (3)
- (c) Show that the tangent to the curve at the point where  $t = \frac{\pi}{6}$  has the equation

$$2x + 3\sqrt{3} y = 9. {3}$$

(d) Find a cartesian equation for the curve in the form  $y^2 = f(x)$ . (4)

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